

LECTURE 27 – HIGH SPEED OP AMPS

LECTURE ORGANIZATION

Outline

- Extending the GB of conventional op amps
- Cascade Amplifiers
 - Voltage amplifiers
 - Voltage amplifiers using current feedback
- Summary

CMOS Analog Circuit Design, 3rd Edition Reference

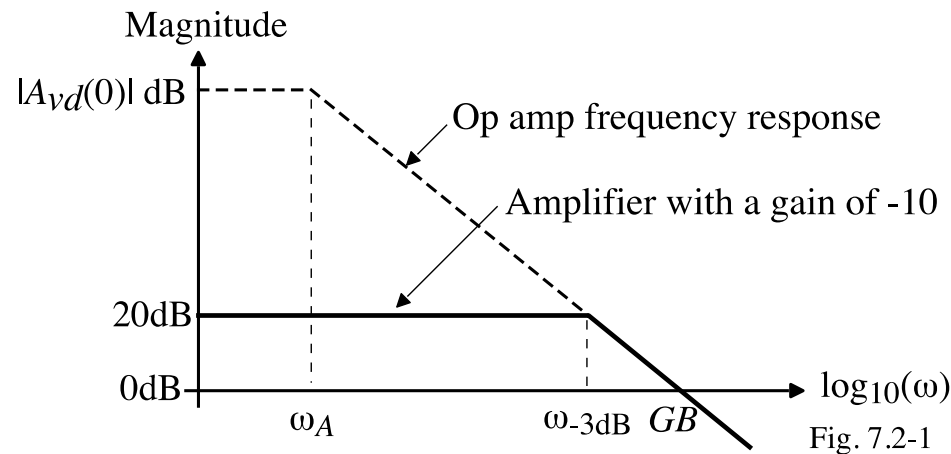
Pages 370-386

INCREASING THE GB OF OP AMPS

What is the Influence of GB on the Frequency Response?

The unity-gainbandwidth represents a limit in the trade-off between closed loop voltage gain and the closed-loop -3dB frequency.

Example of a gain of -10 voltage amplifier:



What defines the GB ?

We know that

$$GB = \frac{g_m}{C}$$

where g_m is the transconductance that converts the input voltage to current and C is the capacitor that causes the dominant pole.

This relationship assumes that all higher-order poles are greater than GB .

What is the Limit of GB?

The following illustrates what happens when the next higher pole is not greater than GB :

For a two-stage op amp, the poles and zeros are:

1.) Dominant pole
$$p_1 = \frac{-g_{m1}}{A_v(0)C_c}$$

2.) Output pole
$$p_2 = \frac{-g_{m6}}{C_L}$$

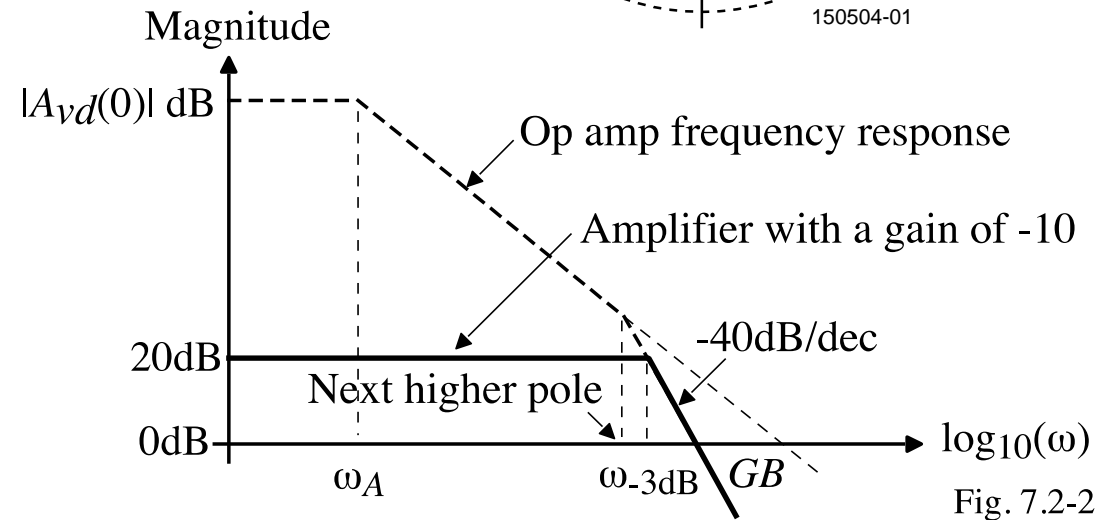
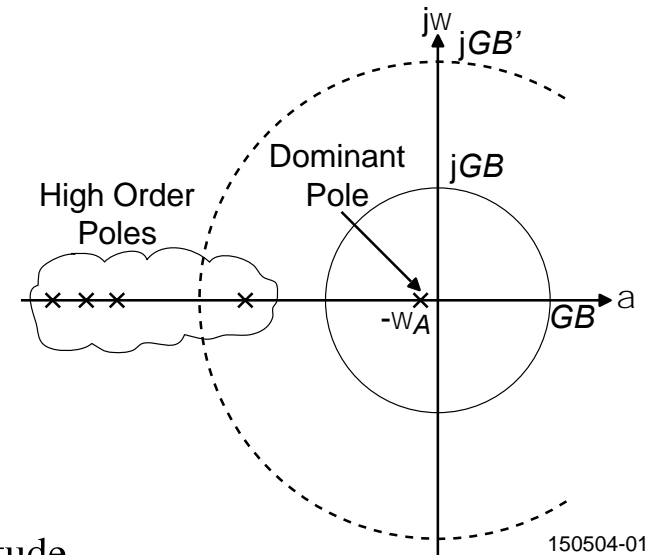
3.) Mirror pole
$$p_3 = \frac{-g_{m3}}{C_{gs3} + C_{gs4}}$$

and

$$z_3 = 2p_3$$

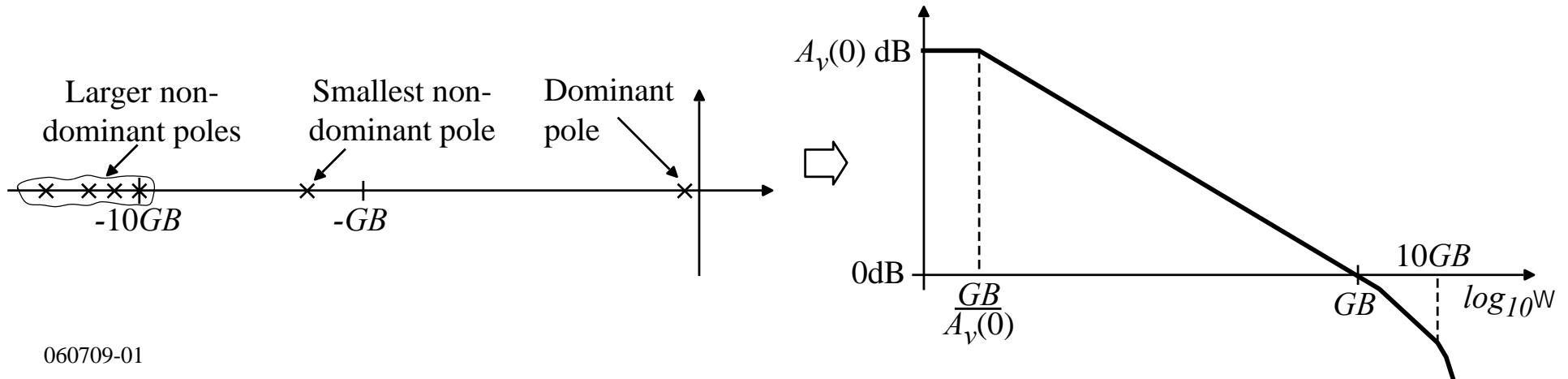
4.) Nulling pole
$$p_4 = \frac{-1}{R_z C_I}$$

5.) Nulling zero
$$z_1 = \frac{-1}{R_z C_c - (C_c/g_{m6})}$$



Higher-Order Poles

For reasonable phase margin, the smallest higher-order pole should be 2-3 times larger than GB if all other higher-order poles are larger than $10GB$.



If the higher-order poles are not greater than $10GB$, then the distance from GB to the smallest non-dominant pole should be increased for reasonable phase margin.

Increasing the GB of a Two-Stage Op Amp

- 1.) Use the nulling zero to cancel the closest pole beyond the dominant pole.
- 2.) The maximum GB would be equal to the magnitude of the second closest pole beyond the dominant pole.
- 3.) Adjust the dominant pole so that $2.2GB \approx$ (second closest pole beyond the dominant pole)

Illustration which assumes that p_2 is the next closest pole beyond the dominant pole:

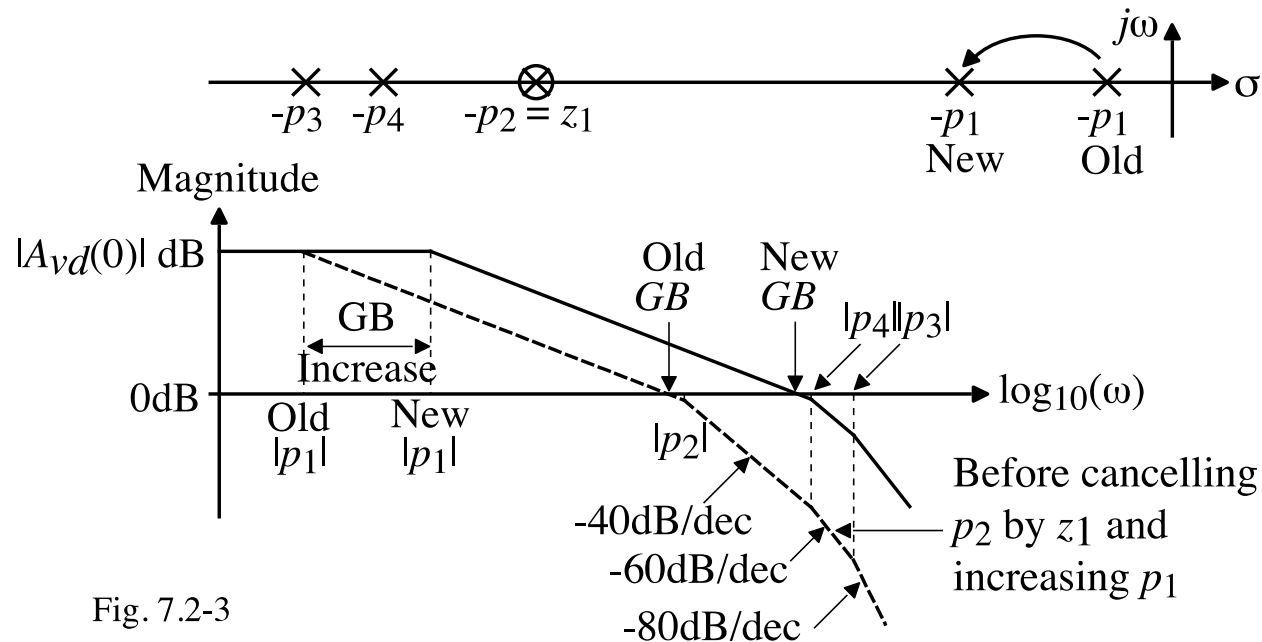


Fig. 7.2-3

Example 27-1 - Increasing the GB of the Op Amp Designed in Ex. 23-1

Use the two-stage op amp designed in Examples 23-1 and 23-2 and apply the above approach to increase the gainbandwidth as much as possible. Use the capacitor values in the table shown along with $C_{ox} = 6\text{fF}/\mu\text{m}^2$.

Solution

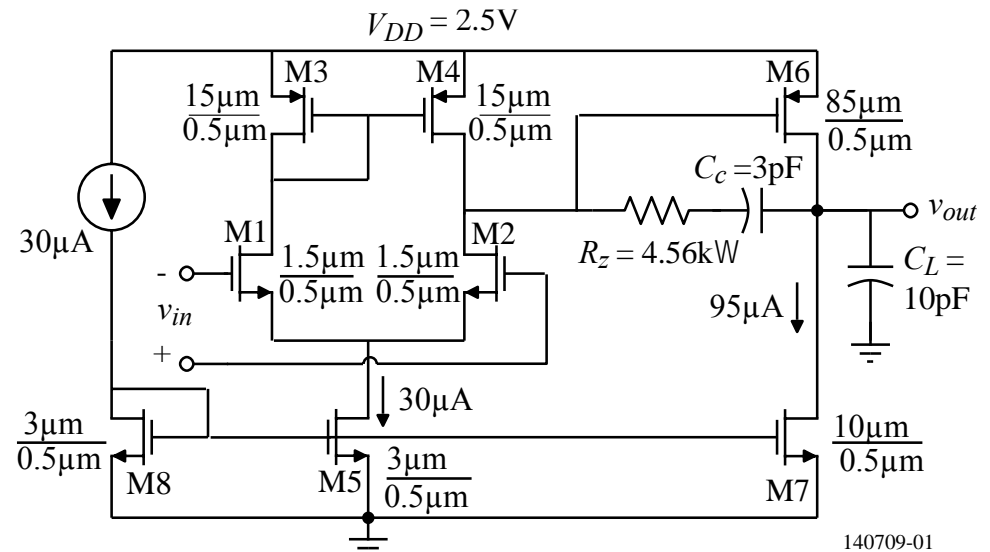
1.) First find the values of p_2 , p_3 , and p_4 .

a.) From Ex. 23-2, we see that

$$p_2 = -95 \times 10^6 \text{ rads/sec.}$$

b.) p_3 was found in Ex. 23-1 as

$$p_3 = -1.25 \times 10^9 \text{ rads/sec. (also there is a zero at } -2.5 \times 10^9 \text{ rads/sec.)}$$



Type	P-Channel	N-Channel	Units
CGSO	220×10^{-12}	220×10^{-12}	F/m
CGDO	220×10^{-12}	220×10^{-12}	F/m
CGBO	700×10^{-12}	700×10^{-12}	F/m
CJ	560×10^{-6}	770×10^{-6}	F/m ²
CJSW	350×10^{-12}	380×10^{-12}	F/m
MJ	0.5	0.5	
MJSW	0.35	0.38	

Example 27-1 - Continued

(c.) To find p_4 , we must find C_I which is the output capacitance of the first stage of the op amp. C_I consists of the following capacitors,

$$C_I = C_{bd2} + C_{bd4} + C_{gs6} + C_{gd2} + C_{gd4}$$

For C_{bd2} the width is $1.5\mu\text{m} \Rightarrow L1+L2+L3=3\mu\text{m} \Rightarrow AS/AD=4.5\mu\text{m}^2$ and $PS/PD=9\mu\text{m}$.

For C_{bd4} the width is $15\mu\text{m} \Rightarrow L1+L2+L3=3\mu\text{m} \Rightarrow AS/AD=45\mu\text{m}^2$ and $PS/PD=36\mu\text{m}$.

From Table 3.2-1:

$$C_{bd2} = (4.5\mu\text{m}^2)(770 \times 10^{-6}\text{F/m}^2) + (9\mu\text{m})(380 \times 10^{-12}\text{F/m}) = 3.47\text{fF} + 3.42\text{fF} \approx 6.89\text{fF}$$

$$C_{bd4} = (45\mu\text{m}^2)(560 \times 10^{-6}\text{F/m}^2) + (36\mu\text{m})(350 \times 10^{-12}\text{F/m}) = 25.2\text{fF} + 12.6\text{fF} \approx 37.8\text{fF}$$

C_{gs6} in saturation is,

$$\begin{aligned} C_{gs6} &= CGDO \cdot W_6 + 0.67(C_{ox}W_6L_6) = (220 \times 10^{-12})(85 \times 10^{-6}) + (0.67)(6 \times 10^{-15})(42.5) \\ &= 18.7\text{fF} + 255\text{fF} = 273.7\text{fF} \end{aligned}$$

$$C_{gd2} = 220 \times 10^{-12} \times 1.5\mu\text{m} = 0.33\text{fF} \text{ and } C_{gd4} = 220 \times 10^{-12} \times 15\mu\text{m} = 3.3\text{fF}$$

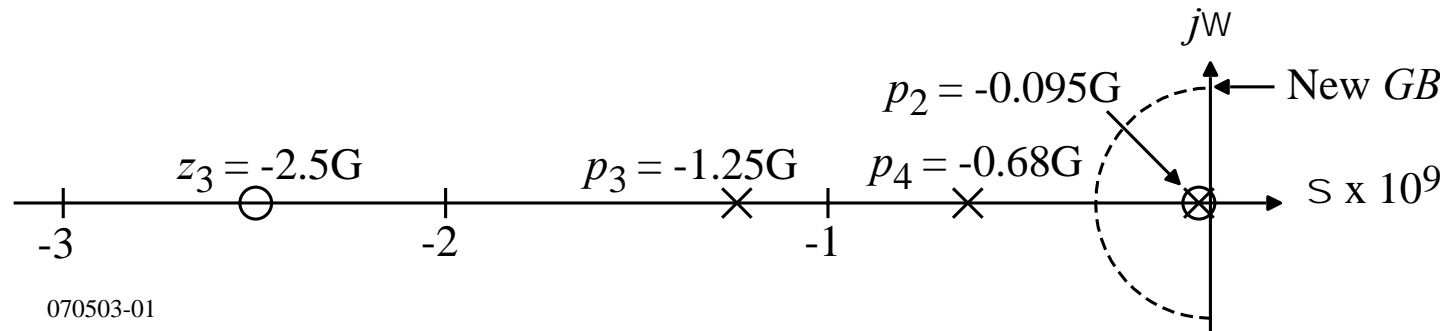
Therefore, $C_I = 6.9\text{fF} + 37.8\text{fF} + 273.7\text{fF} + 0.33\text{fF} + 3.3\text{fF} = 322\text{fF}$. Although C_{bd2} and C_{bd4} will be reduced with a reverse bias, let us use these values to provide a margin.

Thus let C_I be 322fF.

In Ex. 23-2, R_z was $4.564\text{k}\Omega$ which gives $p_4 = -0.680 \times 10^9$ rads/sec.

Example 27-1 - Continued

Therefore, the roots are:



When p_2 is cancelled, the next smaller pole is p_4 which will define the new GB . 2.)

Using the nulling zero, z_1 , to cancel p_2 , gives p_4 as the next smallest pole.

For 60° phase margin $GB = |p_4|/2.2$ if the next smallest pole is more than $10GB$.

$$\therefore GB = 0.680 \times 10^9 / 2.2 = 0.309 \times 10^9 \text{ rads/sec. or } 49.2 \text{ MHz.}$$

This value of GB is designed from the relationship that $GB = g_{m1}/C_c$. Assuming g_{m1} is constant, then $C_c = g_{m1}/GB = (94.25 \times 10^{-6}) / (0.309 \times 10^9) = 307 \text{ fF}$. It might be useful to increase g_{m1} in order to keep C_c above the surrounding parasitic capacitors ($C_{gd6} = 18.7 \text{ fF}$). The success of this method assumes that there are no other roots with a magnitude smaller than $10GB$.

The result of this example is to increase the GB from 5 MHz to 49 MHz .

Example 27-2 - Increasing the GB of the Folded Cascode

Use the folded-cascode op amp designed in Example 24-4 and apply the above approach to increase the gainbandwidth as much as possible. Assume that the drain/source areas are equal to $2\mu\text{m}$ times the width of the transistor and that all voltage dependent capacitors are at zero voltage.

Solution

The poles of the folded cascode op amp are:

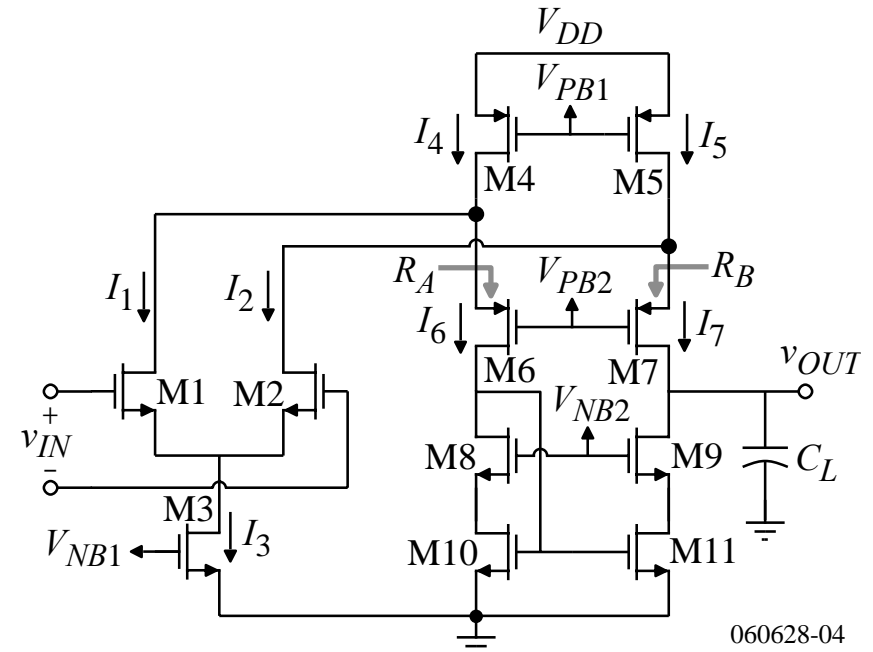
$$p_A \approx \frac{-1}{R_A C_A} \quad (\text{the pole at the source of M6})$$

$$p_B \approx \frac{-1}{R_B C_B} \quad (\text{the pole at the source of M7})$$

$$p_6 \approx \frac{-g_{m10}}{C_6} \quad (\text{the pole at the drain of M6})$$

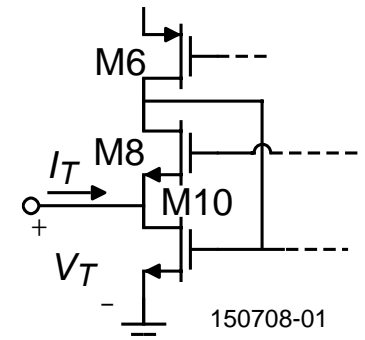
$$p_8 \approx \frac{-g_{m8} r_{ds8} g_{m10}}{C_8} \quad (\text{the pole at the source of M8})$$

$$p_9 \approx \frac{-g_{m9}}{C_9} \quad (\text{the pole at the source of M9})$$



$$I_T = g_{m8} V_T r_{ds8} g_{m10}$$

$$R_8 = \frac{V_T}{I_T} = \frac{1}{g_{m8} r_{ds8} g_{m10}}$$



Example 27-2 - Continued

Let us evaluate each of these poles.

1.) For p_A , the resistance R_A is approximately equal to g_{m6} and C_A is given as

$$C_A = C_{gs6} + C_{bd1} + C_{gd1} + C_{bd4} + C_{bs6} + C_{gd4}$$

From Ex. 24-4, $g_{m6} = 774.6\mu\text{S}$ and capacitors giving C_A are found as,

$$C_{gs6} = (220 \times 10^{-12} \cdot 80 \times 10^{-6}) + (0.67)(80\mu\text{m} \cdot 0.5\mu\text{m} \cdot 6\text{fF}/\mu\text{m}^2) = 177.6\text{fF}$$

$$C_{bd1} = (770 \times 10^{-6})(16.5 \times 10^{-6} \cdot 2 \times 10^{-6}) + (380 \times 10^{-12})(37 \times 10^{-6}) = 39.5\text{fF}$$

$$C_{gd1} = (220 \times 10^{-12} \cdot 16.5 \times 10^{-6}) = 3.6\text{fF}$$

$$C_{bd4} = C_{bs6} = (560 \times 10^{-6})(80 \times 10^{-6} \cdot 2 \times 10^{-6}) + (350 \times 10^{-12})(2 \cdot 82 \times 10^{-6}) = 147\text{fF}$$

and

$$C_{gd4} = (220 \times 10^{-12})(80 \times 10^{-6}) = 17.6\text{fF}$$

Therefore,

$$C_A = 177.6\text{fF} + 39.5\text{fF} + 3.6\text{fF} + 147\text{fF} + 17.6\text{fF} + 147\text{fF} = 0.532\text{pF}$$

Thus,

$$p_A = \frac{-774.6 \times 10^{-6}}{0.532 \times 10^{-12}} = -1.456 \times 10^9 \text{ rads/sec.}$$

2.) For the pole, p_B , the capacitance connected to this node is

$$C_B = C_{gd2} + C_{bd2} + C_{gs7} + C_{gd5} + C_{bd5} + C_{bs7}$$

Example 27-2 - Continued

The various capacitors above are found as

$$C_{gd2} = (220 \times 10^{-12} \cdot 16.5 \times 10^{-6}) = 3.6 \text{ fF}$$

$$C_{bd2} = (770 \times 10^{-6})(16.5 \times 10^{-6} \cdot 2 \times 10^{-6}) + (380 \times 10^{-12})(37 \times 10^{-6}) = 39.5 \text{ fF}$$

$$C_{gs7} = (220 \times 10^{-12} \cdot 80 \times 10^{-6}) + (0.67)(80 \mu\text{m} \cdot 0.5 \mu\text{m} \cdot 6 \text{ fF}/\mu\text{m}^2) = 177.6 \text{ fF}$$

$$C_{gd5} = (220 \times 10^{-12})(80 \times 10^{-6}) = 17.6 \text{ fF}$$

and

$$C_{bd5} = C_{bs7} = (560 \times 10^{-6})(80 \times 10^{-6} \cdot 2 \times 10^{-6}) + (350 \times 10^{-12})(2 \cdot 82 \times 10^{-6}) = 147 \text{ fF}$$

The value of C_B is the same as C_A and g_{m6} is assumed to be the same as g_{m7} giving $p_B = p_A = -1.456 \times 10^9$ rads/sec.

3.) For the pole, p_6 , the capacitance connected to this node is

$$C_6 = C_{bd6} + C_{gd6} + C_{gs10} + C_{gs11} + C_{bd8} + C_{gd8}$$

The various capacitors above are found as

$$C_{bd6} = (560 \times 10^{-6})(80 \times 10^{-6} \cdot 2 \times 10^{-6}) + (350 \times 10^{-12})(2 \cdot 82 \times 10^{-6}) = 147 \text{ fF}$$

$$C_{gs10} = C_{gs11} = (220 \times 10^{-12} \cdot 10 \times 10^{-6}) + (0.67)(10 \mu\text{m} \cdot 0.5 \mu\text{m} \cdot 6 \text{ fF}/\mu\text{m}^2) = 22.2 \text{ fF}$$

$$C_{bd8} = (770 \times 10^{-6})(10 \times 10^{-6} \cdot 2 \times 10^{-6}) + (380 \times 10^{-12})(2 \cdot 12 \times 10^{-6}) = 24.5 \text{ fF}$$

$$C_{gd8} = (220 \times 10^{-12})(10 \times 10^{-6}) = 2.2 \text{ fF} \quad \text{and} \quad C_{gd6} = C_{gd5} = 17.6 \text{ fF}$$

Therefore, $C_6 = 147 \text{ fF} + 17.6 \text{ fF} + 22.2 \text{ fF} + 22.2 \text{ fF} + 2.2 \text{ fF} + 17.6 \text{ fF} = 0.229 \text{ pF}$

Example 27-2 - Continued

From Ex. 24-4, $g_{m10} = 600 \times 10^{-6}$. Therefore, p_6 , can be expressed as

$$-p_6 = \frac{600 \times 10^{-6}}{0.229 \times 10^{-12}} = 2.62 \times 10^9 \text{ rads/sec.}$$

4.) Next, we consider the pole, p_8 . The capacitance connected to this node is

$$C_8 = C_{bd10} + C_{gd10} + C_{gs8} + C_{bs8}$$

These capacitors are given as,

$$C_{bs8} = C_{bd10} = (770 \times 10^{-6})(10 \times 10^{-6} \cdot 2 \times 10^{-6}) + (380 \times 10^{-12})(2 \cdot 12 \times 10^{-6}) = 24.5 \text{ fF}$$

$$C_{gs8} = (220 \times 10^{-12} \cdot 10 \times 10^{-6}) + (0.67)(10 \mu\text{m} \cdot 0.5 \mu\text{m} \cdot 6 \text{ fF}/\mu\text{m}^2) = 22.2 \text{ fF}$$

and

$$C_{gd10} = (220 \times 10^{-12})(10 \times 10^{-6}) = 2.2 \text{ fF}$$

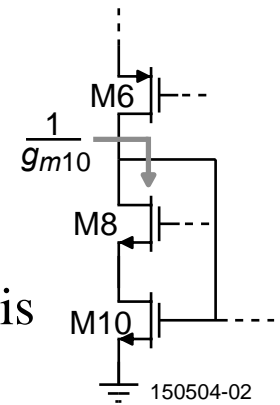
The capacitance C_8 is equal to

$$C_8 = 24.5 \text{ fF} + 2.2 \text{ fF} + 22.2 \text{ fF} + 24.5 \text{ fF} = 73.4 \text{ fF}$$

Using the values of Ex. 24-4 of $600 \mu\text{S}$, the pole p_8 is found as,

$$-p_8 = g_{m8} r_{ds8} g_{m10} / C_8 = -600 \mu\text{S} \cdot 600 \mu\text{S} / 4.5 \mu\text{S} \cdot 73.4 \text{ fF} = -1090 \times 10^9 \text{ rads/sec.}$$

5.) The capacitance for the pole at p_9 is identical with C_8 . Therefore, since g_{m9} is $600 \mu\text{S}$, the pole p_9 is $-p_9 = 8.17 \times 10^9 \text{ rads/sec.}$

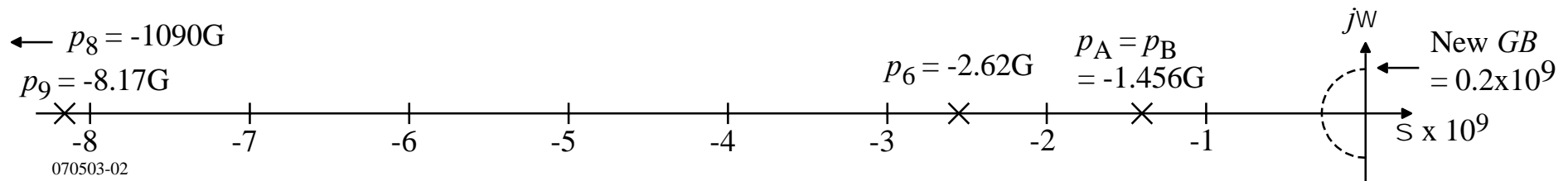


Example 27-2 - Continued

The poles are summarized below:

$$p_A = -1.456 \times 10^9 \text{ rads/sec} \quad p_B = -1.456 \times 10^9 \text{ rads/sec} \quad p_6 = -2.62 \times 10^9 \text{ rads/sec}$$

$$p_8 = -1090 \times 10^9 \text{ rads/sec} \quad p_9 = -8.17 \times 10^9 \text{ rads/sec}$$



The smallest of these poles is p_A or p_B . Since p_6 is not much larger than p_A or p_B , we will find the new GB by dividing p_A or p_B by 4 (which is a guess rather than 2.2) to get 364×10^6 rads/sec. Thus the new GB will be $364/2\pi$ or 58MHz.

Checking our guess gives a phase margin of,

$$PM = 90^\circ - 2 \tan^{-1}(0.364/1.456) - \tan^{-1}(0.364/2.62) = 54^\circ \text{ which is okay}$$

The magnitude of the dominant pole is given as

$$p_{\text{dominant}} = GB/A_{vd}(0) = 364 \times 10^6 / 3,678 = 99,000 \text{ rads/sec.}$$

The value of load capacitor that will give this pole is

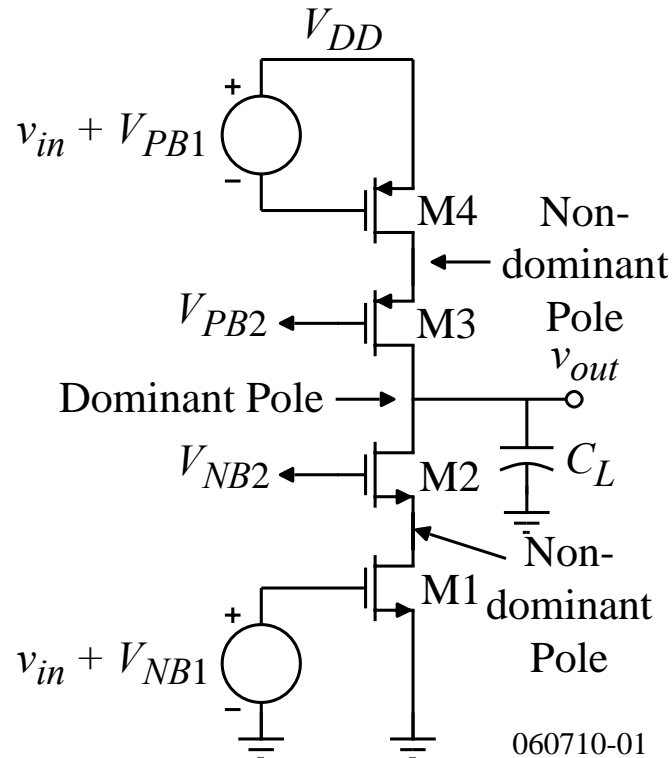
$$C_L = (p_{\text{dominant}} \cdot R_{\text{out}})^{-1} = (99 \times 10^3 \cdot 7.44 \text{M}\Omega)^{-1} = 1.36 \text{pF}$$

Therefore, the new $GB = 58\text{MHz}$ compared with the old $GB = 10\text{MHz}$.

Elimination of Higher-Order Poles

Principle - minimize the number of nodes in the amplifier.

The minimum circuitry for a cascode op amp is shown below:



If the source-drain area between M1 and M2 and M3 and M4 can be minimized, the non-dominant poles will be quite large.

Dynamically Biased, Push-Pull, Cascode Op Amp

Push-pull, cascode amplifier: M1-M2 and M3-M4

Bias circuitry: M5-M6-C₂ and M7-M8-C₁

Operation:

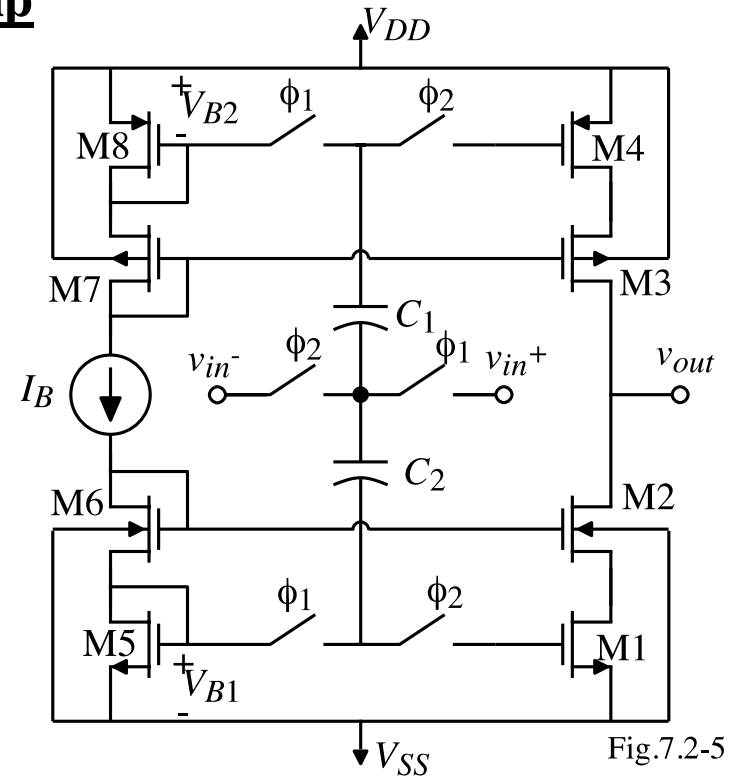
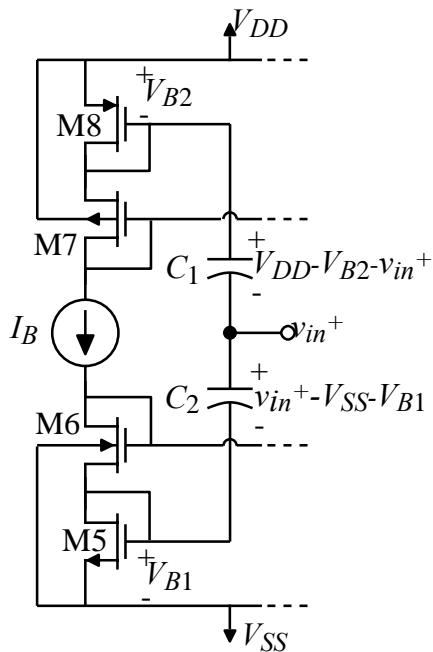
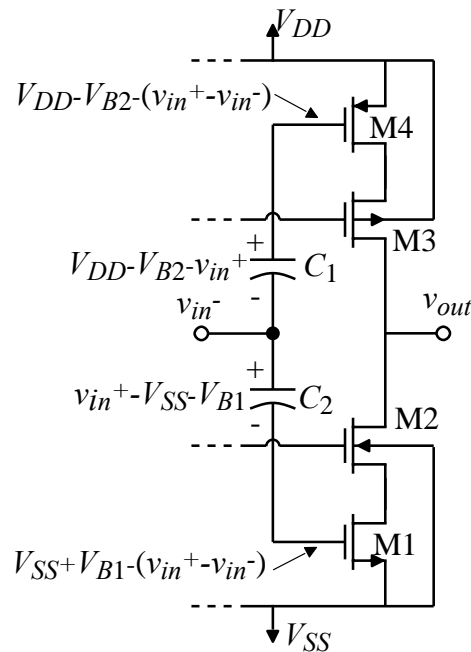


Fig.7.2-5



Equivalent circuit during the ϕ_1 clock period

120523-07



Equivalent circuit during the ϕ_2 clock period.

120523-08

Dynamically Biased, Push-Pull, Cascode Op Amp - Continued

This circuit will operate on both clock phases[†].

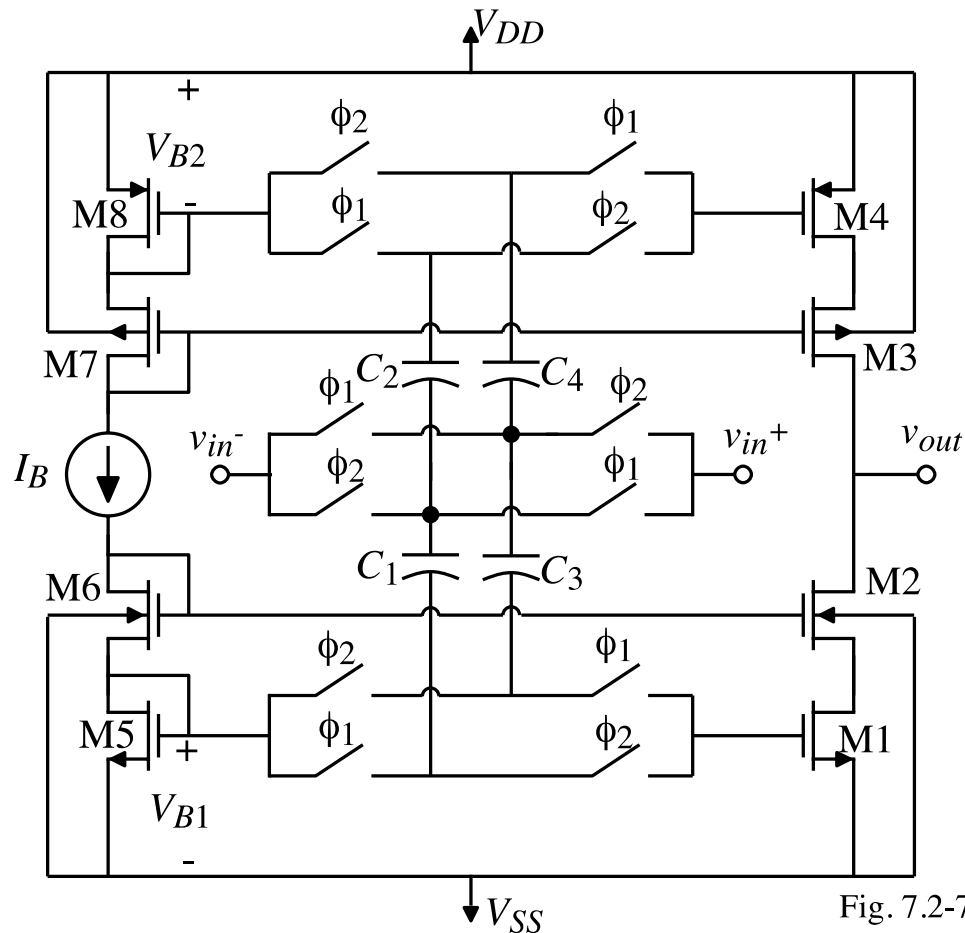


Fig. 7.2-7

Performance (1.5 μ m CMOS):

- 1.6mW dissipation
- $GB \approx 130\text{MHz}$ ($C_L=2.2\text{pF}$)
- Settling time of 10ns ($C_L=10\text{pF}$)

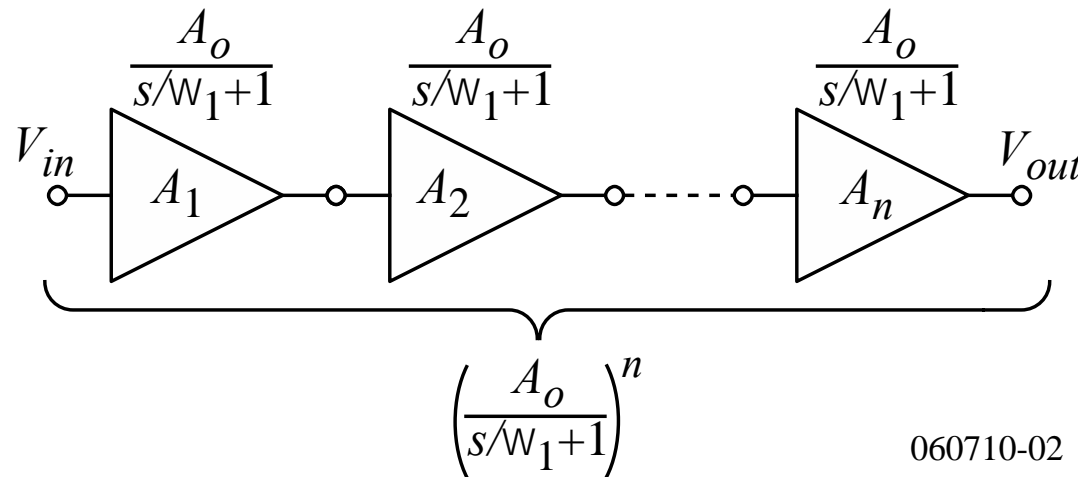
This amplifier was used with a 28.6MHz clock to realize a 5th-order switched capacitor filter having a cutoff frequency of 3.5MHz.

[†] S. Masuda, et. al., "CMOS Sampled Differential Push-Pull Cascode Op Amp," *Proc. of 1984 International Symposium on Circuits and Systems*, Montreal, Canada, May 1984, pp. 1211-12-14.

CASCADED AMPLIFIERS USING VOLTAGE AMPLIFIERS

Bandwidth of Cascaded Amplifiers

Cascading of low-gain, wide-bandwidth amplifiers:



Overall gain is A_o^n

-3dB frequency is,

$$\omega_{-3\text{dB}} = \omega_1 \sqrt{2^{1/n} - 1}$$

If $A_o = 10$, $\omega_1 = 300\pi \times 10^6$ rads/sec. and $n = 3$, then

Overall gain is 60dB and $\omega_{-3\text{dB}} = 0.51 \omega_1 = 480 \times 10^6$ rads/sec. \rightarrow 76.5 MHz

Ex. 27-3 – Continued

$$C_{out} = C_{gs3} + C_{bs3} + C_{bd1} + C_{bd5} + C_{gd1} + C_{gd5} + C_{gs1}(\text{next stage}) \approx C_{gs3} + C_{gs1}$$

Using $C_{ox} = 60.6 \times 10^{-4} \text{ F/m}^2$, we get,

$$C_{out} \approx (2.5 + 2.5) \times 10^{-12} \text{ m}^2 \times 60.6 \times 10^{-4} \text{ F/m}^2 = 30.3 \text{ fF} \rightarrow C_{out} \approx 30 \text{ fF}$$

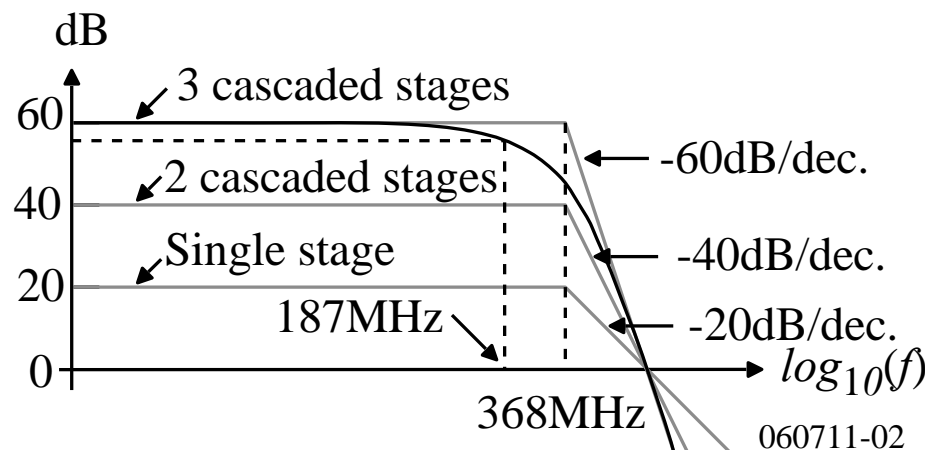
$$g_{m3} = \sqrt{2 \cdot 120 \cdot 1 \cdot 20} \mu\text{S} = 69.3 \mu\text{S}$$

\therefore Dominant pole $\approx 69.3 \mu\text{S} / 30 \text{ fF} = 23.1 \times 10^8 \text{ rads/sec.} \rightarrow f_{-3\text{dB}} = 368 \text{ MHz}$

The bandwidth of three identical cascaded amplifiers giving a low-frequency gain of 60dB would have a $f_{-3\text{dB}}$ of

$$f_{-3\text{dB}}(\text{Overall}) = f_{-3\text{dB}} \sqrt{2^{1/3} - 1} = 368 \text{ MHz} (0.5098) = 187 \text{ MHz.}$$

$$P_{diss} = 3 \text{ mW}$$



CASCADED AMPLIFIERS USING CURRENT FEEDBACK AMPLIFIERS

Advantages of Using Current Feedback

Why current feedback?

- Higher GB
- Less voltage swing \Rightarrow more dynamic range

What is a current amplifier?

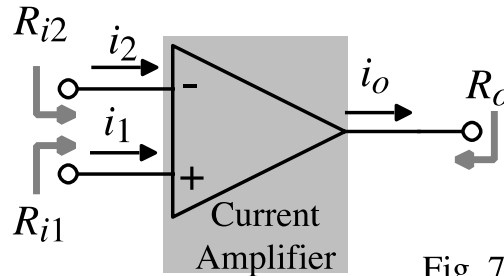


Fig. 7.2-8A

Requirements:

$$i_o = A_i(i_1 - i_2)$$

$$R_{i1} = R_{i2} = 0\Omega$$

$$R_o = \infty$$

Ideal source and load requirements:

$$R_{source} = \infty$$

$$R_{Load} = 0\Omega$$

Bandwidth Advantage of a Current Feedback Amplifier

Consider the inverting voltage amplifier shown using a current amplifier with negative current feedback:

The output current, i_o , of the current amplifier can be written as

$$i_o = A_i(s)(i_1 - i_2) = -A_i(s)(i_{in} + i_o)$$

The closed-loop current gain, i_o/i_{in} , can be found as

$$\frac{i_o}{i_{in}} = \frac{-A_i(s)}{1 + A_i(s)}$$

However, $v_{out} = i_o R_2$ and $v_{in} = i_{in} R_1$. Solving for the voltage gain, v_{out}/v_{in} gives

$$\frac{v_{out}}{v_{in}} = \frac{i_o R_2}{i_{in} R_1} = \left(\frac{-R_2}{R_1} \right) \left(\frac{A_i(s)}{1 + A_i(s)} \right)$$

If $A_i(s) = \frac{A_o}{(s/\omega_A) + 1}$, then

$$\frac{v_{out}}{v_{in}} = \left(\frac{-R_2}{R_1} \right) \left(\frac{A_o}{1 + A_o} \right) \left(\frac{\omega_A(1 + A_o)}{s + \omega_A(1 + A_o)} \right) \Rightarrow A_v(0) = \frac{-R_2 A_o}{R_1(1 + A_o)} \text{ and } \boxed{\omega_{-3dB} = \omega_A(1 + A_o)}$$

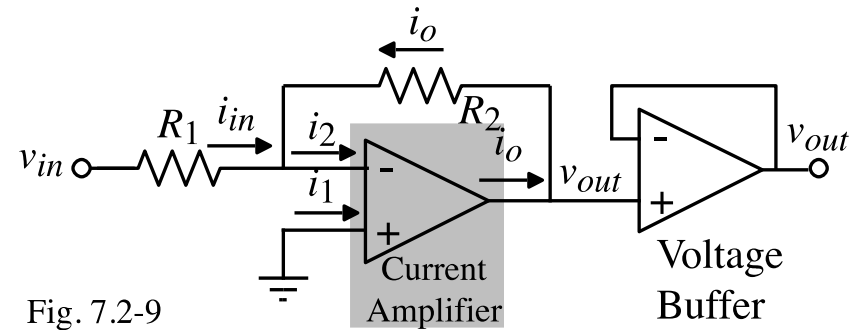


Fig. 7.2-9

Bandwidth Advantage of a Current Feedback Amplifier - Continued

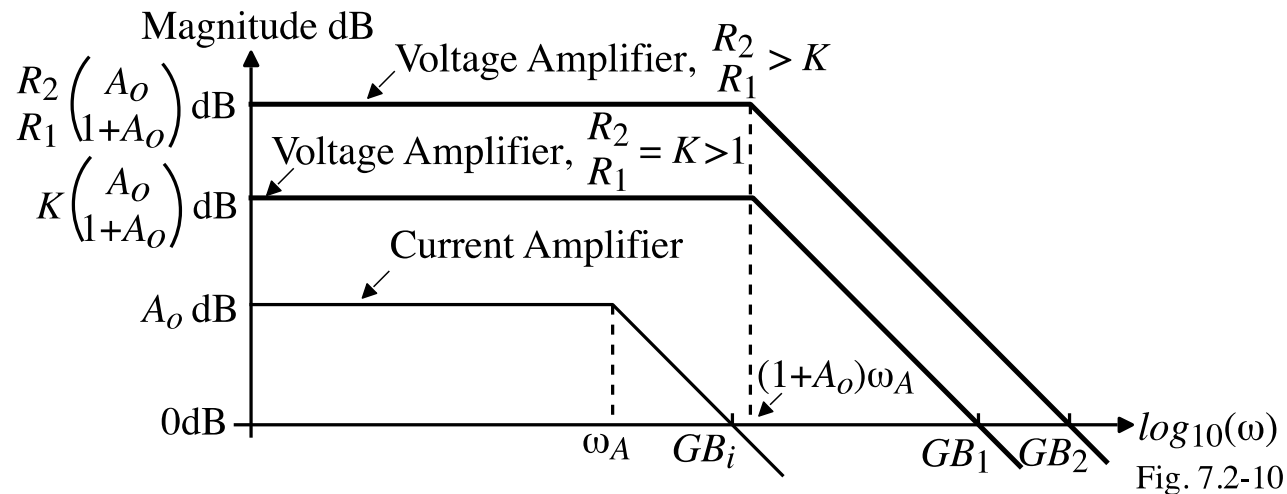
The unity-gainbandwidth is,

$$GB = |A_v(0)| \omega_{-3dB} = \frac{R_2 A_o}{R_1 (1+A_o)} \cdot \omega_A (1+A_o) = \frac{R_2}{R_1} A_o \cdot \omega_A = \frac{R_2}{R_1} GB_i$$

where GB_i is the unity-gainbandwidth of the current amplifier.

Note that if GB_i is constant, then increasing R_2/R_1 (the voltage gain) increases GB .

Illustration:



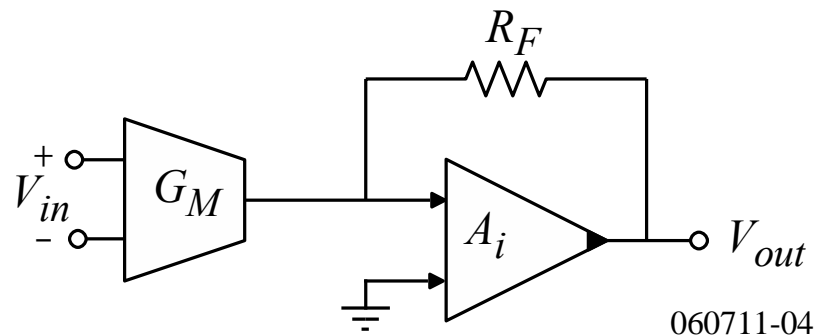
Note that $GB_2 > GB_1 > GB_i$

The above illustration assumes that the GB of the voltage amplifier realizing the voltage buffer is greater than the GB achieved from the above method.

Current Feedback Amplifier

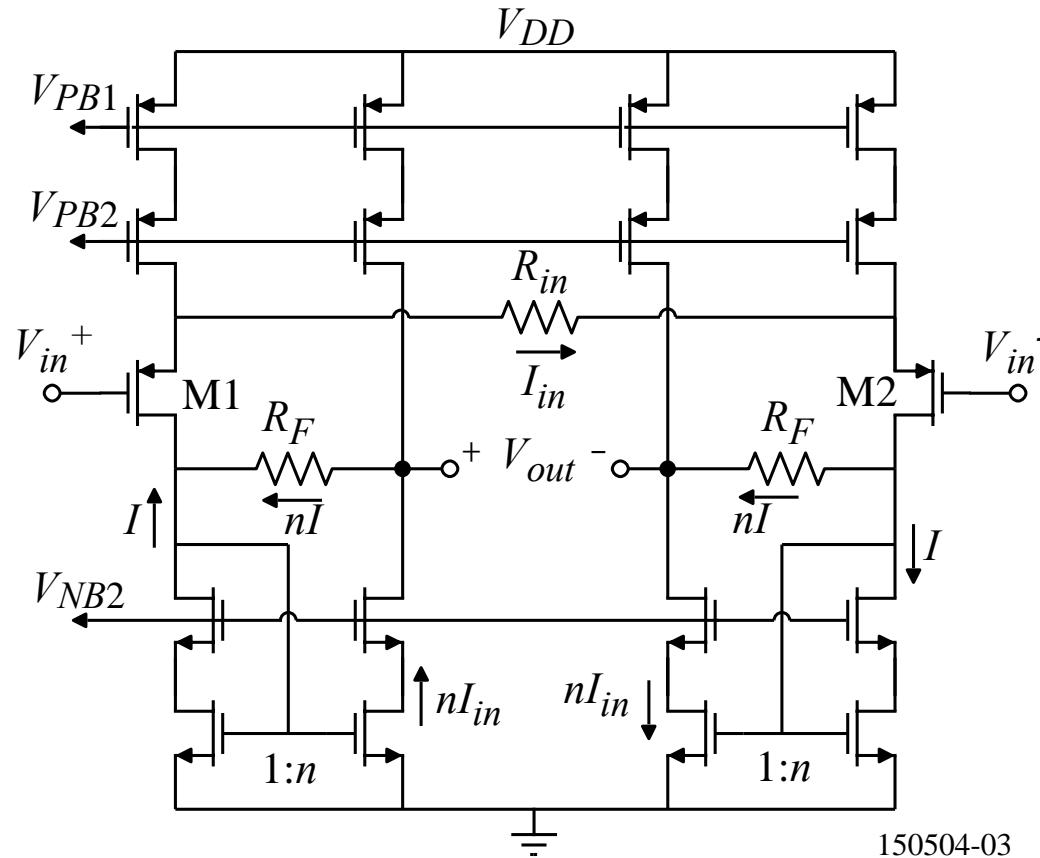
In a current mirror implementation of the current amplifier, it is difficult to make the input resistance sufficiently small compared to R_1 .

This problem can be solved using a transconductance input stage shown in the following block diagram:



$$\frac{V_{out}}{V_{in}} = \frac{-G_M R_F A_i}{1 + A_i}$$

Differential Implementation of the Current Feedback Amplifier



$$I_{in} = \frac{g_{m1}}{1 + 0.5g_{m1}R_{in}} \left(\frac{V_{in}^+ - V_{in}^-}{2} \right), \quad I_{in} = (1+n)I, \quad \text{and} \quad V_{out} = \frac{n(2R_F)}{1+n} I_{in}$$

$$\therefore \frac{V_{out}}{V_{in}} \approx \frac{2nR_F}{(1+n)R_{in}}$$

A 20dB Voltage Amplifier using a Current Amplifier

The following circuit is a programmable voltage amplifier with up to 20dB gain:

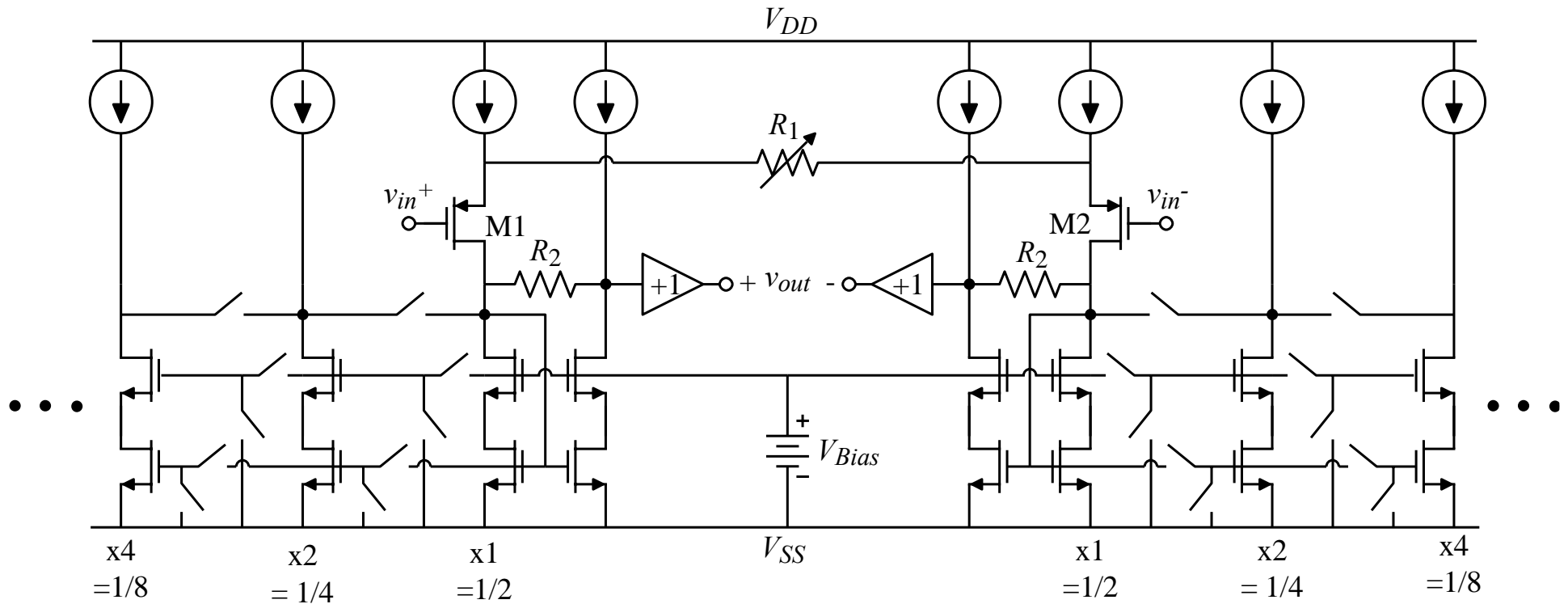
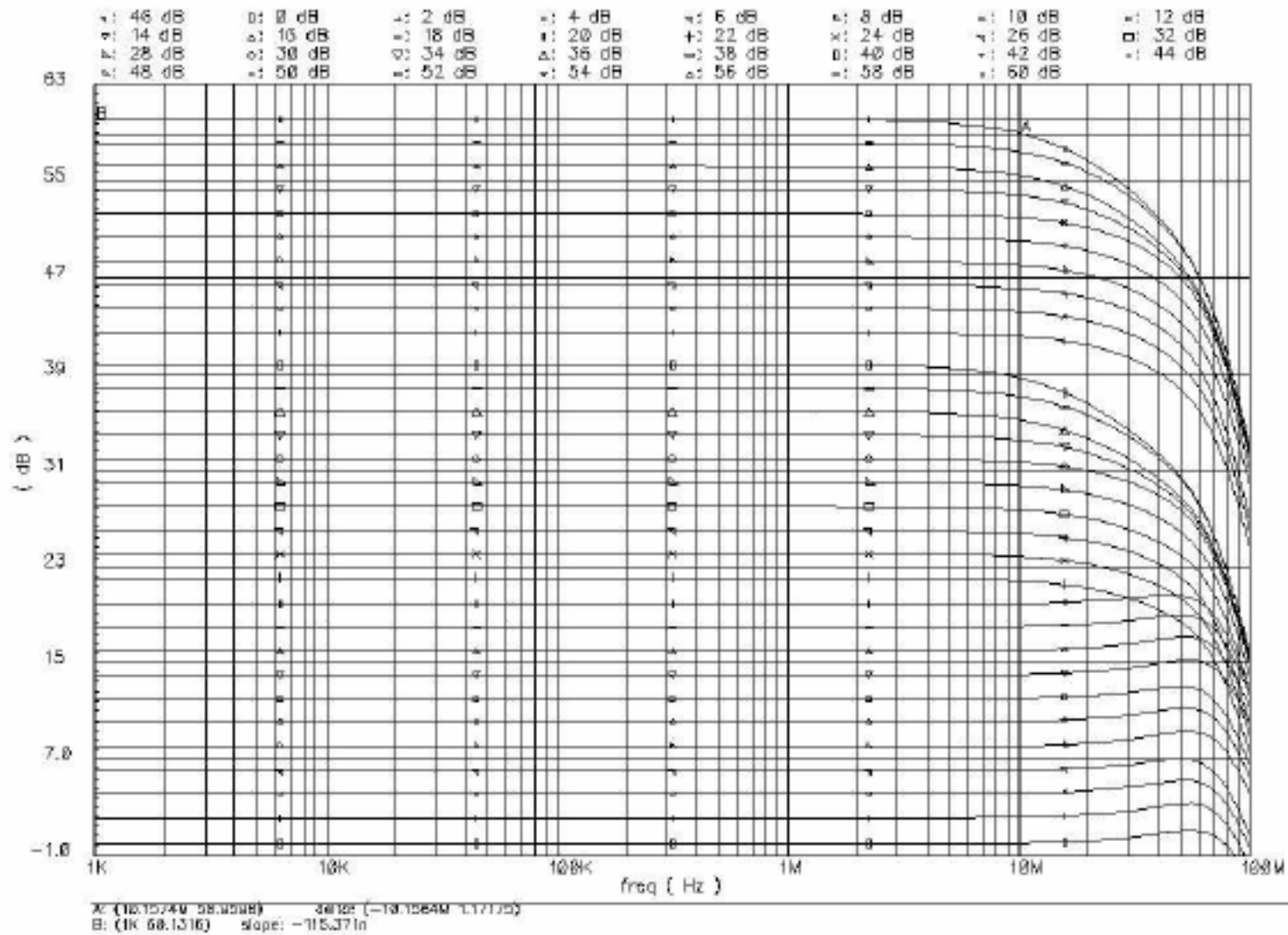


Fig. 7.2-135A

R_1 and the current mirrors are used for gain variation while R_2 is fixed.

Frequency Response of a 60dB PGA

Includes output buffer:



SUMMARY

- Increasing the GB of an op amp requires that the magnitude of all non-dominant poles are much greater than GB from the origin of the complex frequency plane
- The practical limit of GB for an op amp is approximately 5-10 times less than the magnitude of the smallest non-dominant pole ($\approx 100\text{MHz}$)
- To achieve high values of GB it is necessary to eliminate the non-dominant poles (which come from parasitics) or increase the magnitude of the non-dominant poles
- The best way to achieve high-bandwidth amplifiers is to cascade high-bandwidth voltage amplifiers
- If the gain of the high-bandwidth voltage amplifiers is well defined, then it is not necessary to use negative feedback around the amplifier
- Amplifiers with well-defined gains are achievable with a -3dB bandwidth of 100MHz